

On the Physical Basics of Information Flow

C.A.Petri

(modified and presented by Rüdiger Valk)

Results obtained in co-operation with
KONRAD ZUSE
1910 - 1995



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K o m m u n i k a t i o n
m i t
A u t o m a t e n

Von der Fakultät für Mathematik und Physik
der Technischen Hochschule Darmstadt

zur Erlangung des Grades eines
Doktors der Naturwissenschaften
(Dr. rer.nat.)

genehmigte
Dissertation

vorgelegt von
C h r i s t o p h P e t r i
aus Leipzig

Referent: Prof.Dr.rer.techn.A.Walther
Korreferent: Prof.Dr.Ing.E.Unger

Tag der Einreichung: 27.7.1961
Tag der mündlichen Prüfung: 29.6.1962

D 17

honn 1962

information & space

concurrency

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*Petri's general
interest:*

*information processing
&
fundamental laws in
Physics*

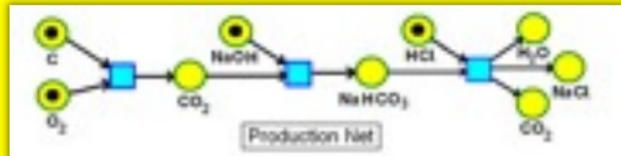
Kommunikation
mit
Automaten

information & space

Von der Fakultät für Mathematik und Physik

da

The graphics, together with the rules for their coarsening and refinement, were invented in August 1939 by Carl Adam Petri - at the age of 13 - for the purpose of describing chemical processes,



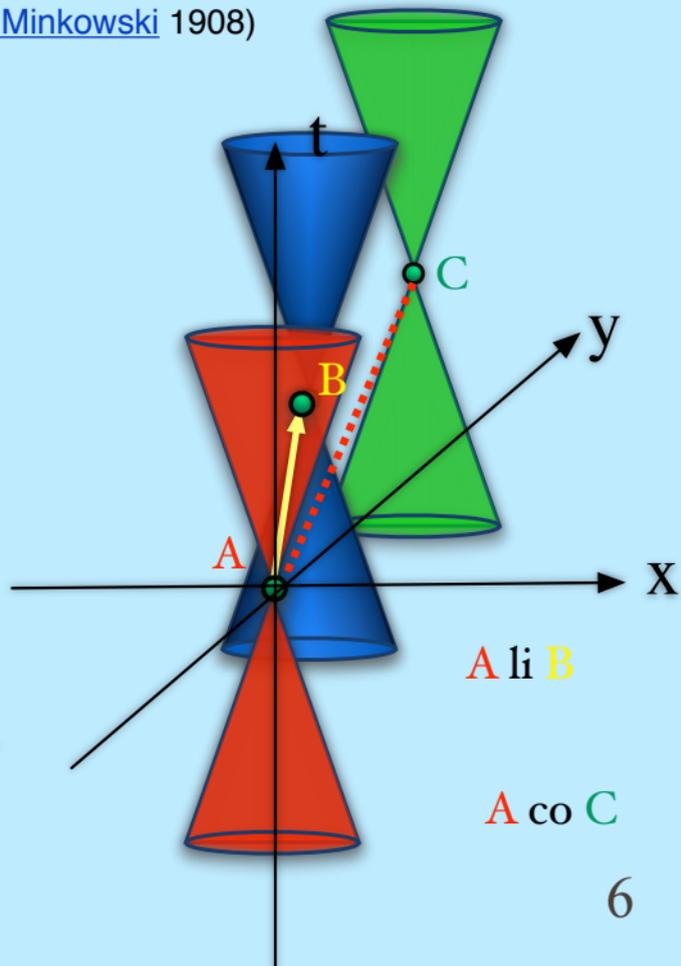
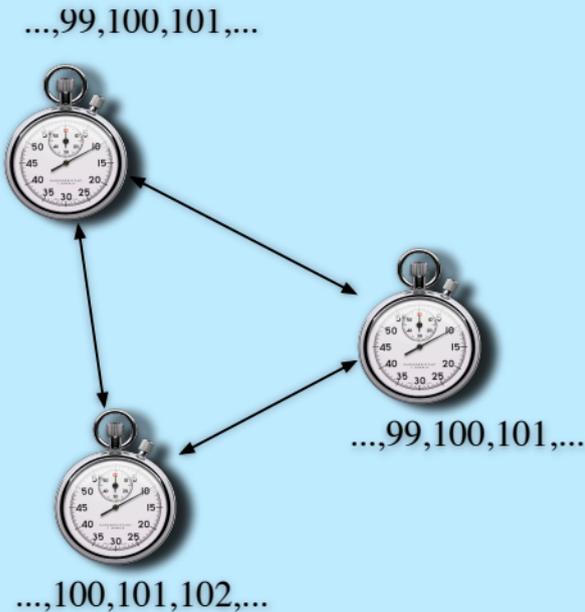
http://www.scholarpedia.org/article/Petri_net

Tag der mündlichen Prüfung: 20.6.1962

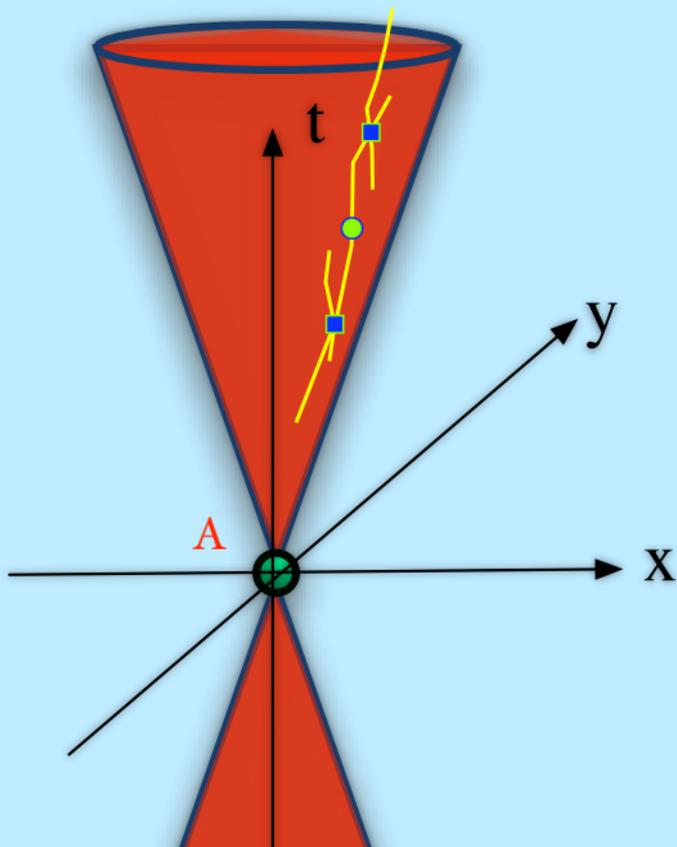
D 17

Juni 1962

Minkowski-Diagrams ([Hermann Minkowski](#) 1908)



Minkowski-Diagrams ([Hermann Minkowski](#) 1908)



Is the Universe a Computer?



The Universe as a big Net

Das Universum als großes Netz

Die Arbeit von Konrad Zuse wurde in den 1960er Jahren mit der Netztheorie verbundener Systeme weiterentwickelt. Dabei gelang es, einige der Einwände gegen Zuses Konzept zuzuräumen.

Von Carl Johan Petri

Während sich Computer von Computern von Leuten kausale Welt, einen großen Teil der Philosophie von gelassen. In den 1960er Jahren, es wurde ein großer Teil der Philosophie von gelassen. In den 1960er Jahren, es wurde ein großer Teil der Philosophie von gelassen.

Die Arbeit von Konrad Zuse wurde in den 1960er Jahren mit der Netztheorie verbundener Systeme weiterentwickelt. Dabei gelang es, einige der Einwände gegen Zuses Konzept zuzuräumen.

schwerer. Was die gelungene, erklärte die Welt als ein großes Netzwerk.

Seine Idee wurde in den 1960er Jahren mit der Netztheorie verbundener Systeme weiterentwickelt. Dabei gelang es, einige der Einwände gegen Zuses Konzept zuzuräumen.

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Carl Johan Petri (links) im Gespräch mit Konrad Zuse, um 1967

Meetings with Zuse

about 1970 - 80

Which tenets?

Zuse: “Those which can be understood by an Engineer“.

Is the universe a gigantic computer?

Which tenets?

Zuse: “Those which can be understood by an Engineer“.

But many years passed before the deterministic approach of Gerard 't Hooft (2002) made a complete elaboration of the originally conceived ideas possible, namely that of

Combinatorial Modelling

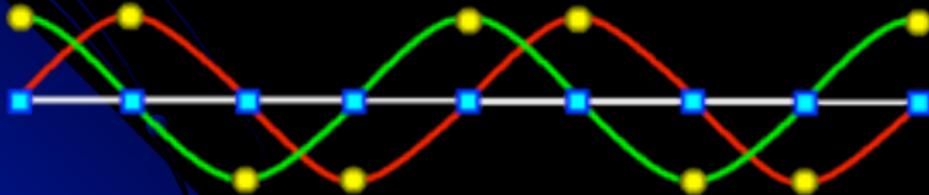
INNOVATIONS

- Revised Order Axioms for Measurement
- Synthesis of „Discrete“ and „Continuous“
- Derivation of Computing Primitives from smallest closed Signal Spaces

Procedure

By means of NET modelling, we translate the main tenets of modern Physics into their **combinatorial form**.

In that form, they are **independent of scale**, and relate to **direct experience** as well as to the **sub-microscopic level of quantum foam**.



Essentials of Net Theory

1. TWO kinds of world points:

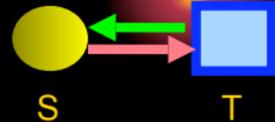
elements: STATES and TRANSITIONS

e.g. Substances and Reactions



2. TWO relations between world points:

arcs: GIVE and TAKE
e.g. Creation and Annihilation



3. TWO kinds of **continuity** expressible:

Mathematical continuity (“connected and compact”)

Experienced continuity (“connected indifference”)

The Framework for Axioms

nets

occurrence

$S \cup T \neq 0$	$S \cap T = 0$
$'x \cup x' \neq 0$	$'x \cap x' = 0$

$E \neq 0$	Sep2 E
$'E = M - M'$	$E' = M' - M$

$f: A \rightarrow A' \cup id$
$f: F \rightarrow F' \cup id$

$T(n+1) = S(n)$
$C(n+1) \cdot C(n) = 0$

net morphism

piles

Net - Topology

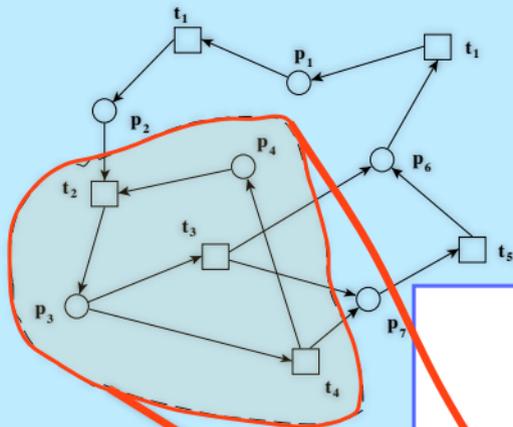


Fig. 2.11. A transition-bordered set

transition bordered

=

closed set

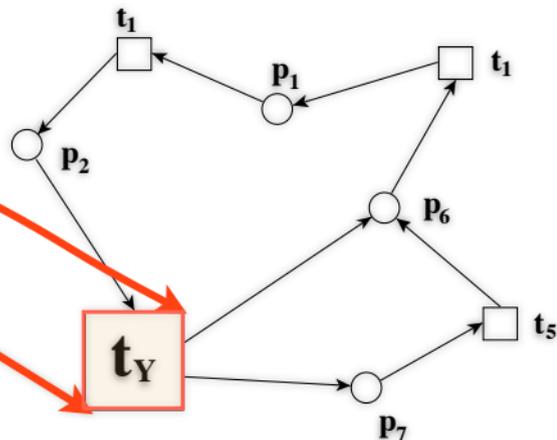


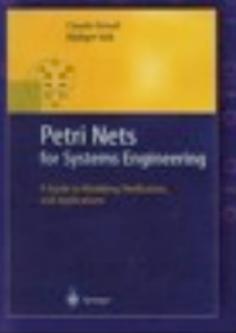
Fig. 2.12. Abstraction from the net of Figure 2.11

系统工程Petri网

——建模、验证与应用指南

Petri Nets for Systems Engineering

A Guide to Modelling, Verification, and Applications



[法] Claude Girault

[德] Rodolphe Valet

王生原 俞 颖 富金健 译
夏安义 审校

是开集又是闭集,例如令 $Y = P \cup T$ 。在这种情况下, Y 到底是被替换为一个库所还是变迁,则是由应用系统的上下文决定的。

在图 2.11 所示的网系统中,集合 $Y = \{p_3, p_4, t_3, t_4\}$ 是一个变迁边界集合,可以将其抽象为一个变迁 t_y ,从而得到一个新的网系统,如图 2.12 所示。下面我们给出这个抽象操作的形式化定义:

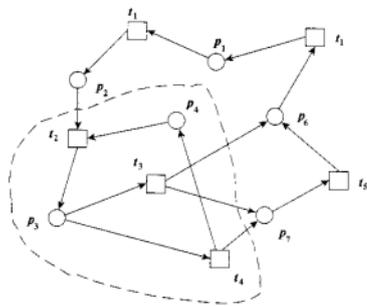


图 2.11 变迁边界集合示例

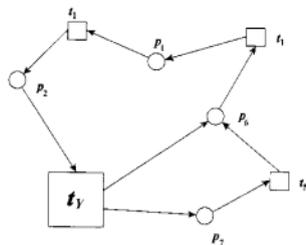


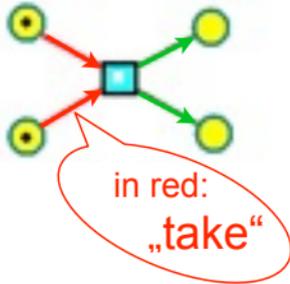
图 2.12 抽象之后的网模型

② 开集和闭集定义了网的拓扑,其中表示了元素和其相邻元素的图形化结构。

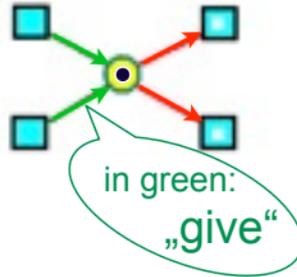
1 Open and closed sets define a topology for a net, which formalises the notion of vicinity of elements with respect to the graphical structure.

The Elements Used in Construction

collection

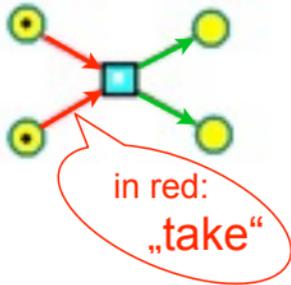


decision

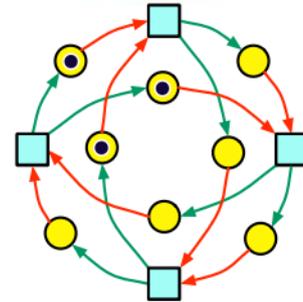
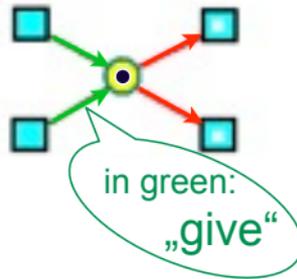


The Elements Used in Construction

collection



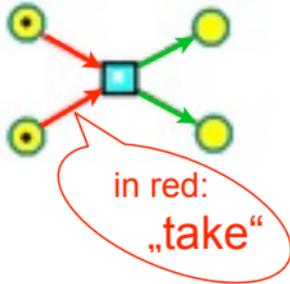
decision



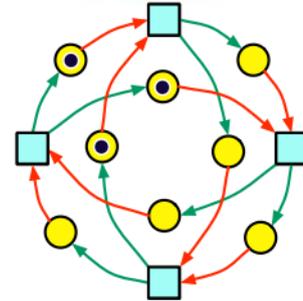
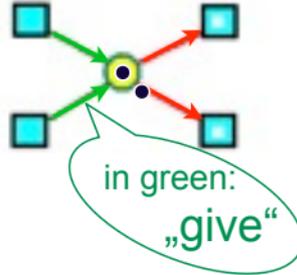
Oscillator

The Elements Used in Construction

collection

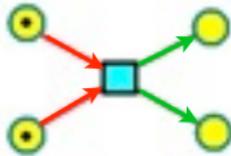


decision



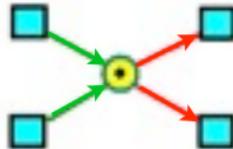
Oscillator

NET TOPOLOGY



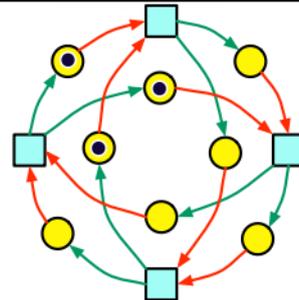
open subnet

The transition is completed by four states



closed subnet

The state is completed by four transitions

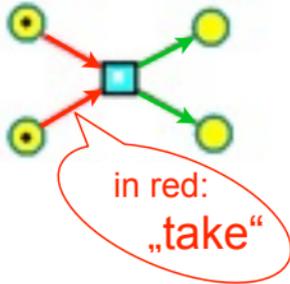


open subnet

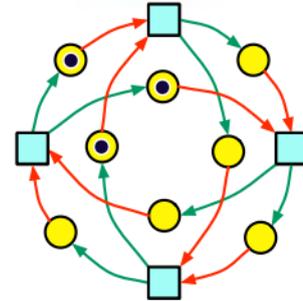
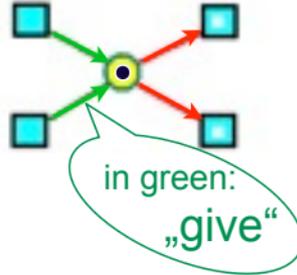
The eight uncompleted states form the border

The Elements Used in Construction

collection

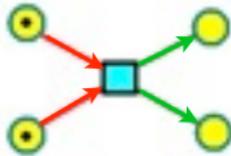


decision



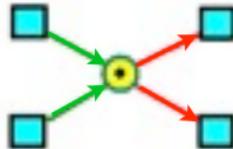
Oscillator

NET TOPOLOGY



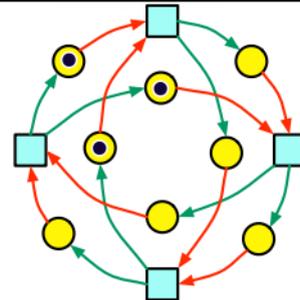
open subnet

The transition is
completed by
four states



closed subnet

The state is
completed by
four transitions



open subnet

The eight uncompleted
states form the border

Measurement

in the classical sense
as related to
the Uncertainty Principle

Four Theses on Measurement

- Every act of Measurement occurs in a Time Window.
- Measurement is, in essence, equivalent to Counting. *)
- Continuous change (e.g. motion) goes unnoticed if not articulated by perceptible non-zero changes.
- Counting leads to a unique result only if the set of objects to be counted and the Time Window are under complete control.

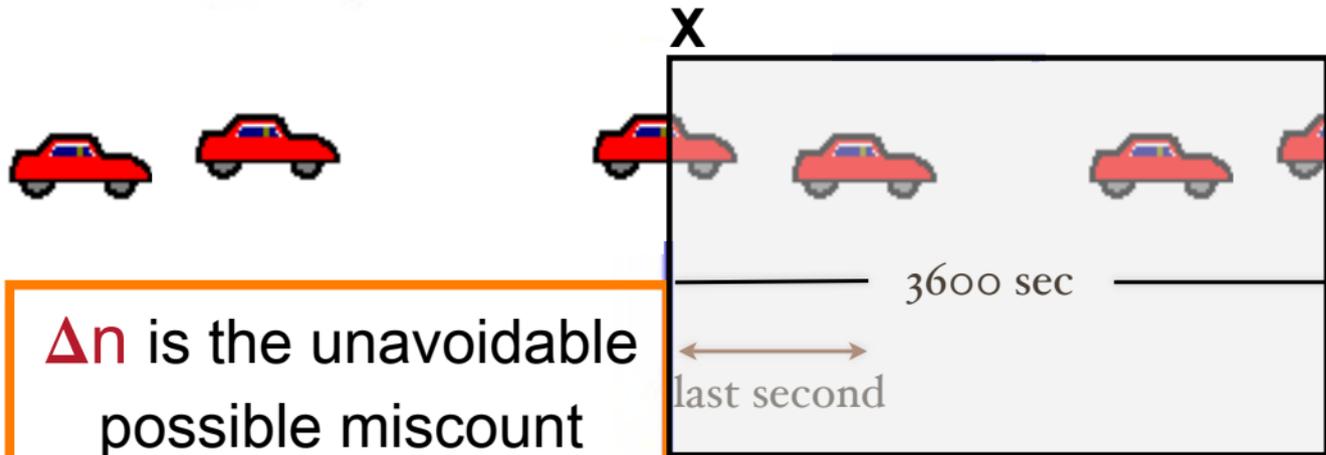
*) SI: 1 second := 9 192 631 770 periods (^{133}Cs line) 25

Law of Uncertainty of Counting

of independent events:

$$\Delta n \geq 1$$

Traffic Statistics: How many cars pass point X in one hour?



Δn is the unavoidable possible miscount

names

1

2

3

4

5

6

7 ...

scale



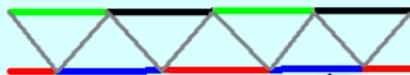
object
indicator



reading:
"4 or 5"

Classical Scale

combinatorial image:



observable states
beyond observation
observable states

momentum p
position q

Correspondence to Heisenberg's Law:



Choice of Observer

He can observe either p or q

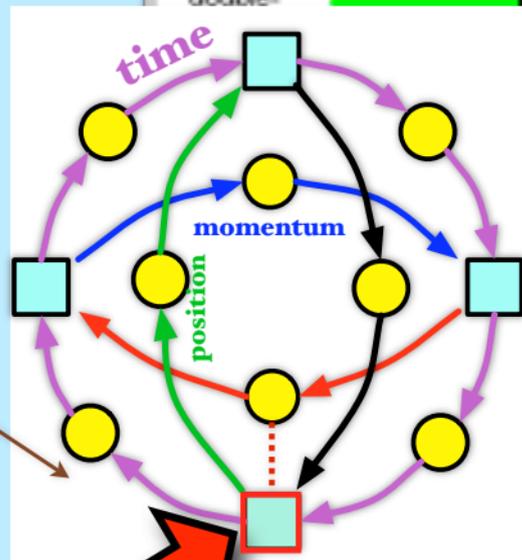
When the position is distinct, the momentum is indistinct etc

names double-



reading:
"4.5"

oscillator



The Main Principles of Modern Physics

$$c = c'$$

Invariance Speed of Light

$$\Delta p \cdot \Delta x \geq h/4\pi$$

Uncertainty Relation

$$E = mc^2$$

Equivalence of Energy and Mass

$$E = h\nu$$

Quantization of Energy

Relativity

Quantum Physics

$$x' = \frac{(x - vt)}{\sqrt{1 - \frac{v^2}{c^2}}} \quad y' = y \quad z' = z \quad t' = \frac{(t - \frac{vx}{c^2})}{\sqrt{1 - \frac{v^2}{c^2}}} \quad n$$

$$\mathbf{x}' = L(\mathbf{x} - \mathbf{v}t)$$

$$t' = L(t - \mathbf{w}\mathbf{x})$$

Invariance Speed of Light

no mention of c !

$$L = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$w := \frac{v}{c^2}$$

slowness

$$\left[\frac{\text{sec}}{\text{m}} \right]$$

These results pertain also to macroscopic levels!

Slowness Effects



This motion proceeds fastest if there is just one gap in front.

Otherwise, we define SLOWNESS w as the quotient

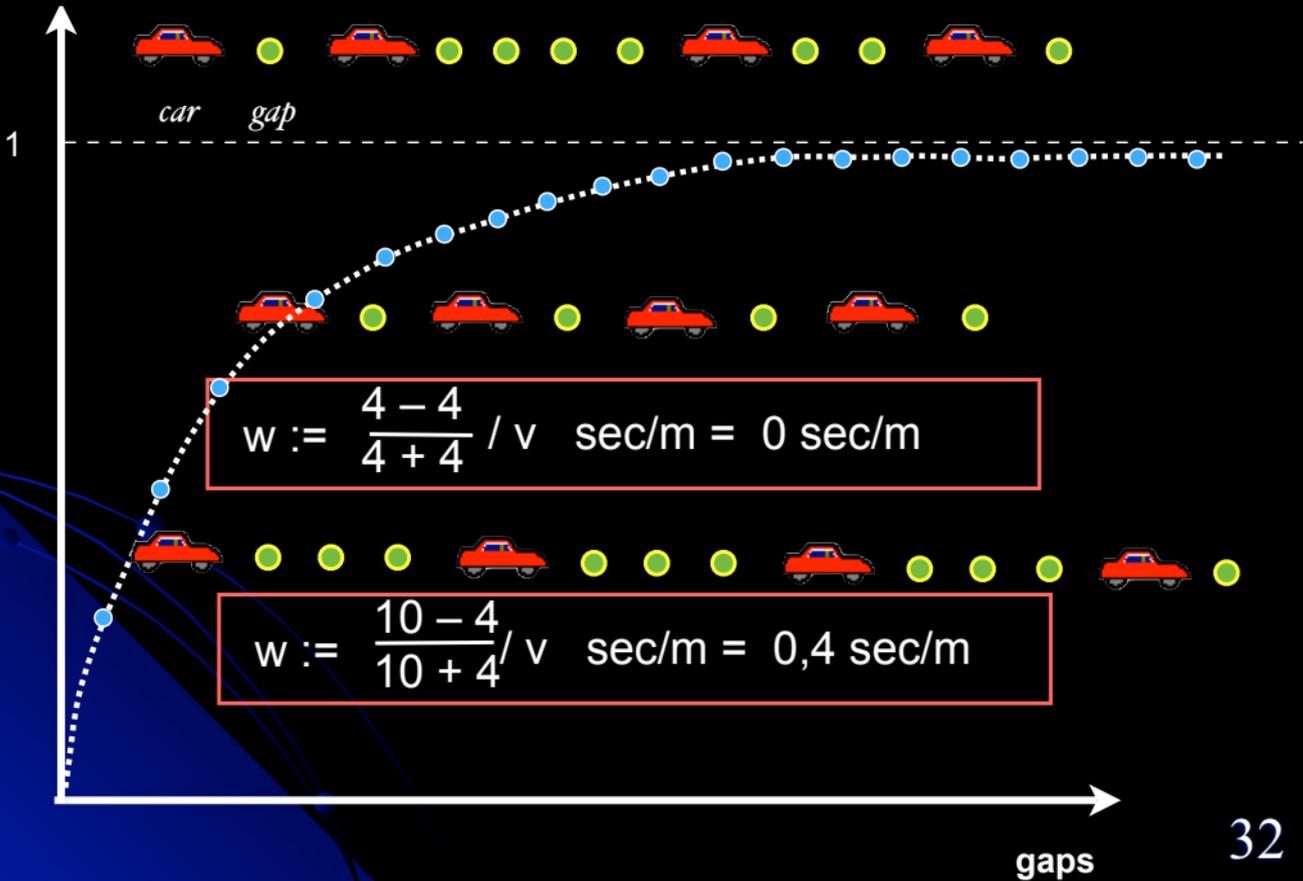
$$w := \frac{\text{gaps} - \text{cars}}{\text{gaps} + \text{cars}} / v \text{ (cars)} \quad \text{sec/m}$$

$$w := \frac{8 - 4}{8 + 4} / v \text{ sec/m} = 1/3 \text{ sec/m}$$

The concept of slowness is a key to understanding repetitive GROUP behaviour. It can be applied to Organization, to Work Flow (**Just-in-time Production**), and to Physical Systems. 31

Slowness Effects

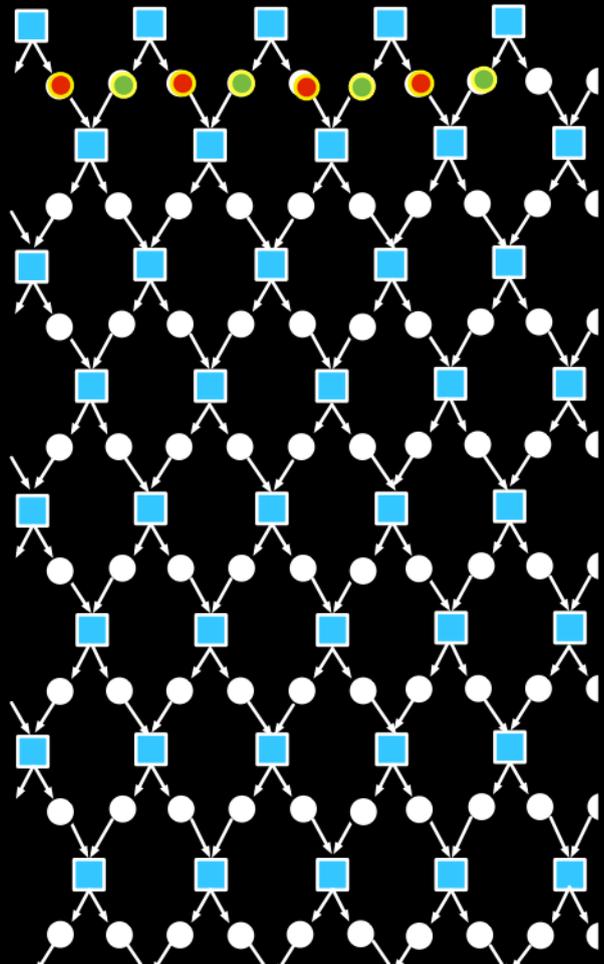
w(gaps)





x

● cars
● gaps



from
Minkowski Space

to

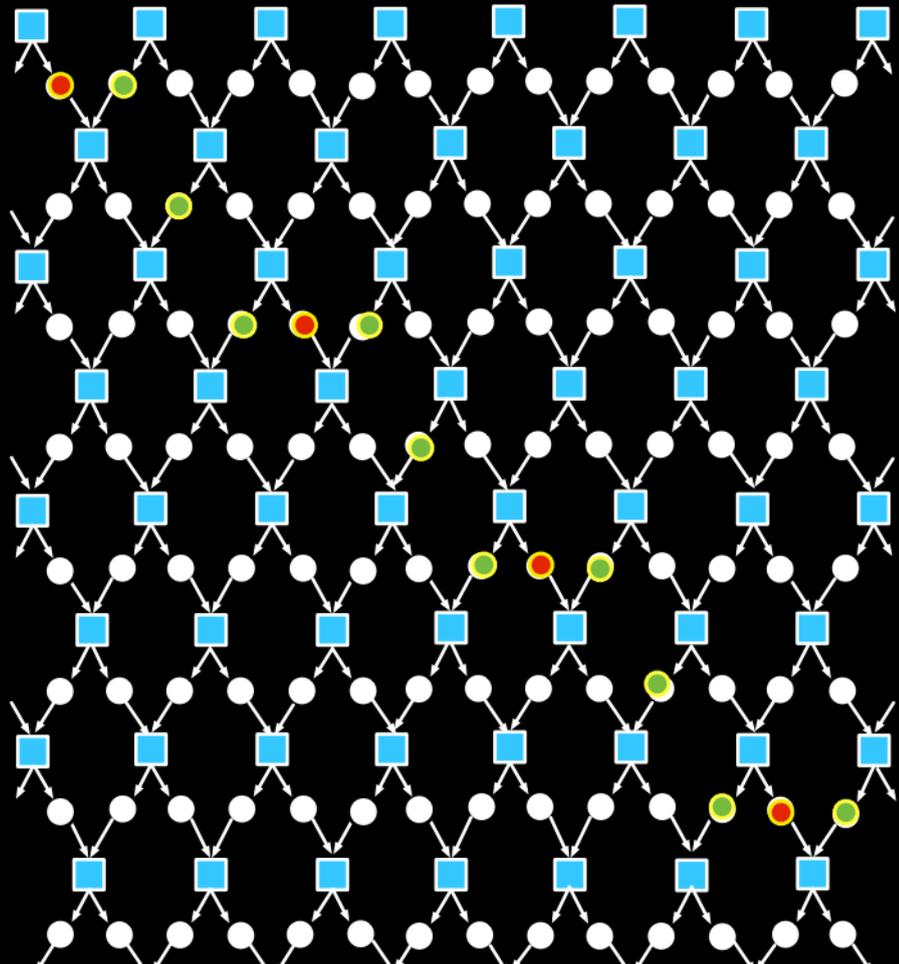
**Petri's
„natural coordinates“**

$$w = 0$$



x

cars
gaps



$w = 0.5$

t

We saw:

The concept of SLOWNESS has its origin in Physics:

It appears in the symmetrical Lorentz Transformation

$$x' := L(x - v t); \quad t' := L(t - w x); \quad w := v / c^2$$

w is measured in seconds (lost) per meter

v is measured in meters (gained) per second

It is the inverse $w = 1 / u$ of the superluminal phase velocity u of material waves, and it is relevant to the movement of electrons in a semiconductor as they interchange places with gaps.



Hence, we saw an example of translation to macroscopic level.

Determinism

Petri and Zuse saw no chance to implement their **deterministic** approach to Information on the level of Quantum Mechanics, because Observation and Measurement have unpredictable outcomes there.

Therefore, they ended the co-operation.

Re-started in 2002:

Petri saw a new chance for completing their work by following the guidelines of Nobel Laureate Gerard 't Hooft who proposes a **deterministic** model on an essentially finer scale.



Gerard 't Hooft

writes in „Determinism beneath Quantum Mechanics“ (2002):

“Contrary to common belief, it is not difficult to construct deterministic models where stochastic behaviour is correctly described by quantum mechanical amplitudes, in precise accordance with the Copenhagen-Bohr-Bohm doctrine.”



Gerard 't Hooft

writes in „Determinism beneath Quantum Mechanics“ (2002):

“Theories of this kind would not only be appealing from a philosophical point of view, but may also be essential for understanding causality at Planckian distance scales.



Gerard 't Hooft

Conclusions of Gerard 't Hooft:

Our view towards the quantum mechanical nature of the world can be summarized as follows:

**Nature's fundamental laws are defined at the Planck scale.
At that scale, all we have is bits of information.**



Determinism excludes the **Creation** of Information.

We (Petri) go one **tentative** step further and forbid the **Destruction** of Information, in order to establish a

Law of Conservation of Information

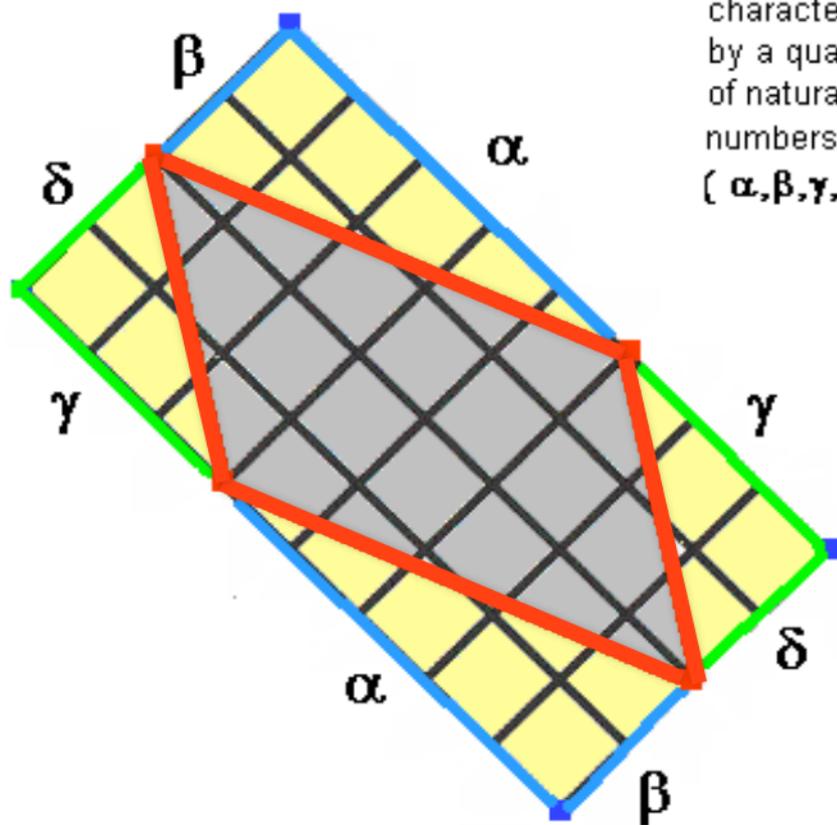
as a prototype of Conservation Laws in general.

Accordingly, we describe the physical Universe in terms of **Signal Flow** and – equivalently – of **Information Flow**.

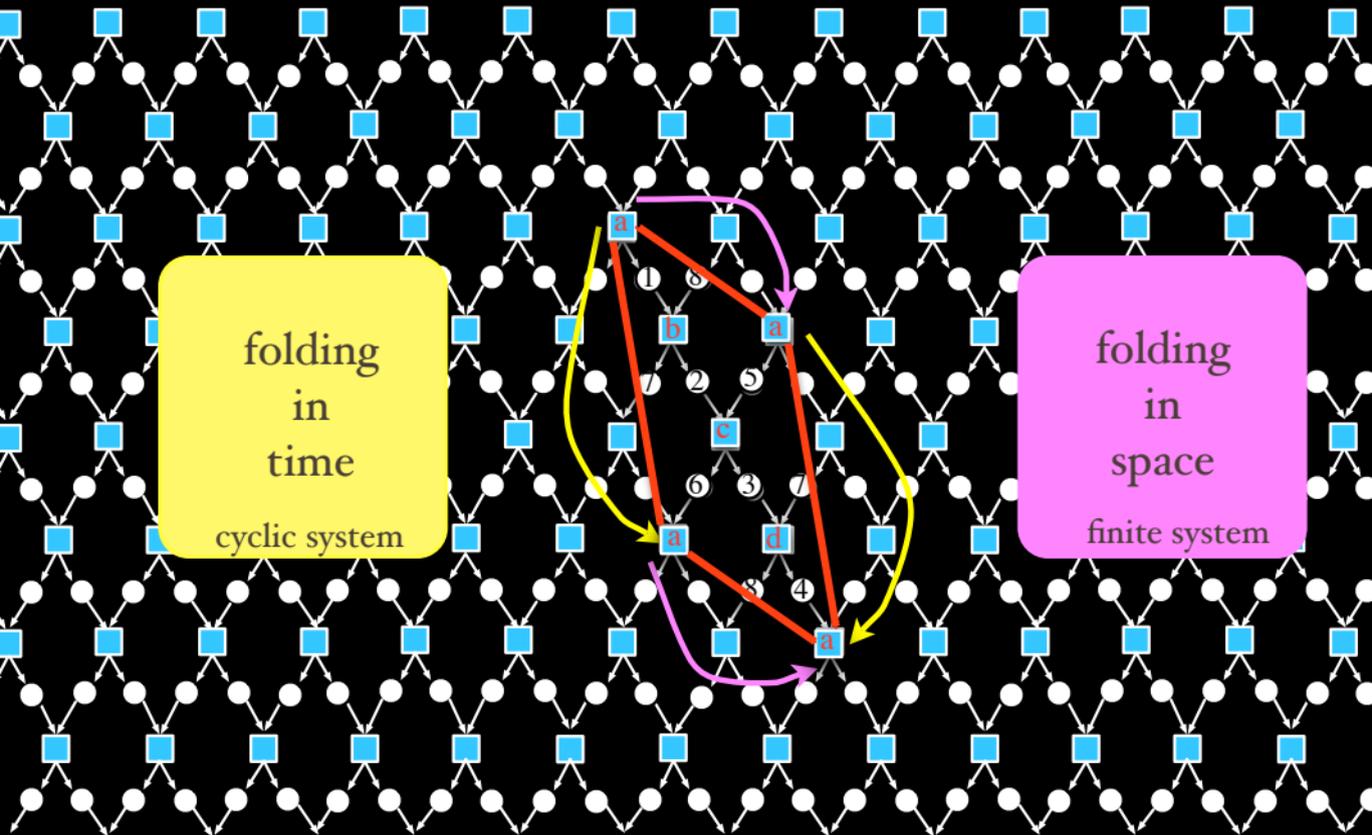
We derive the **Information Operators** from the idea of space-time periodic movement of Signals in an

INTEGER MINKOWSKI SPACE
Petri's „natural coordinates“

Repetitive
behaviour is
characterized
by a quadruple
of natural
numbers:
($\alpha, \beta, \gamma, \delta$)



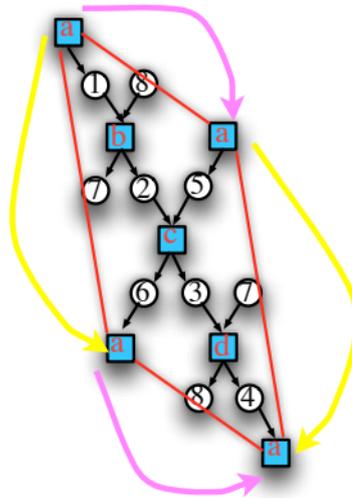
Petri's „natural coordinates“



Petri's „natural coordinates“

folding
in
time

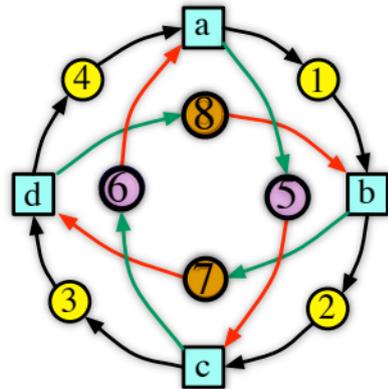
cyclic system



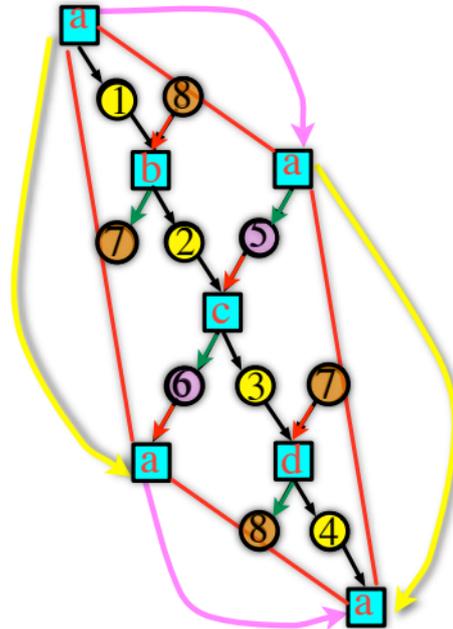
folding
in
space

finite system

Petri's „natural coordinates“



Oscillator!



Folding the Space-Time image of a parallelogram to a „Cycloid“ represents signal movement periodic in space and time.

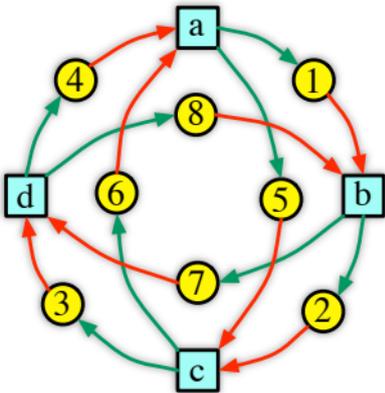
Petri's „natural coordinates“

New orientation of arrows!

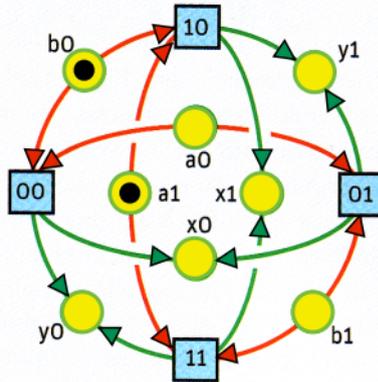
$$x = a$$

$$y = a \text{ XOR } b$$

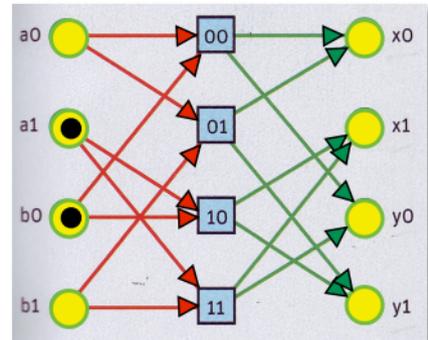
Exclusive OR



oscillator



=



isomorphic graph

We derive the **Information Operators** from the idea of space-time periodic movement of Signals in an **INTEGER MINKOWSKI SPACE**

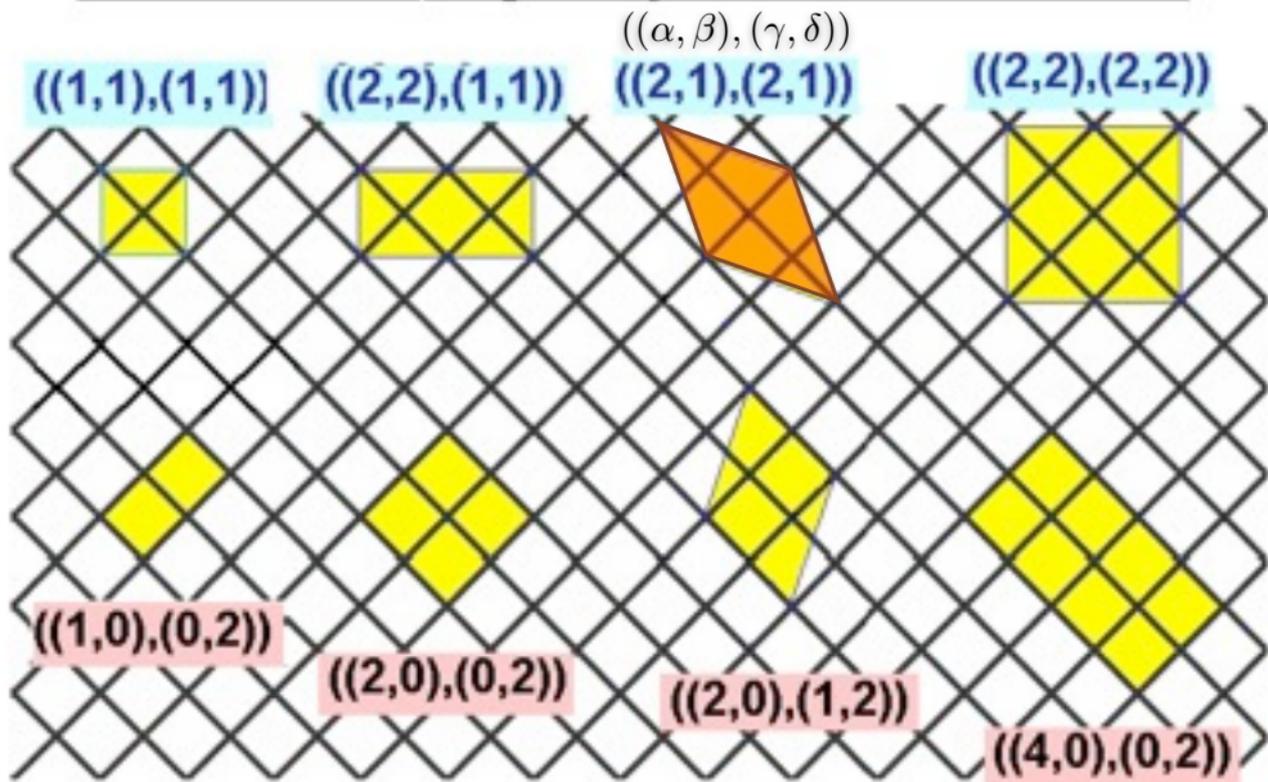
A central idea of Combinatorial Modelling:

We use the **Trajectories of Particles**



as **NATURAL COORDINATES**

The smallest regular patterns of behavior



The smallest lossfree Boolean Transfer

$$((\alpha, \beta), (\gamma, \delta))$$

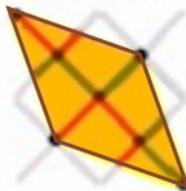
Bit-pair-Equality



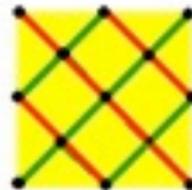
Synchronizer, Bit Exchange



XOR-Transfer



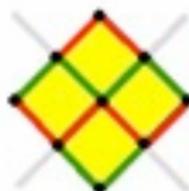
Majority Transfer



$$((4, 0), (0, 2))$$



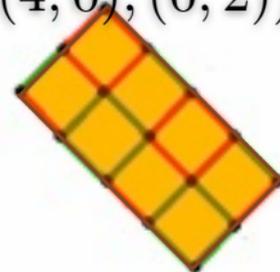
Dual of the two-state Automaton (not a net!)



Synchronizer, Bit Exchange

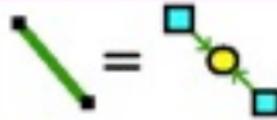
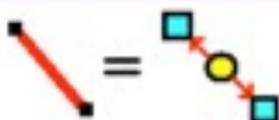


XOR-Transfer

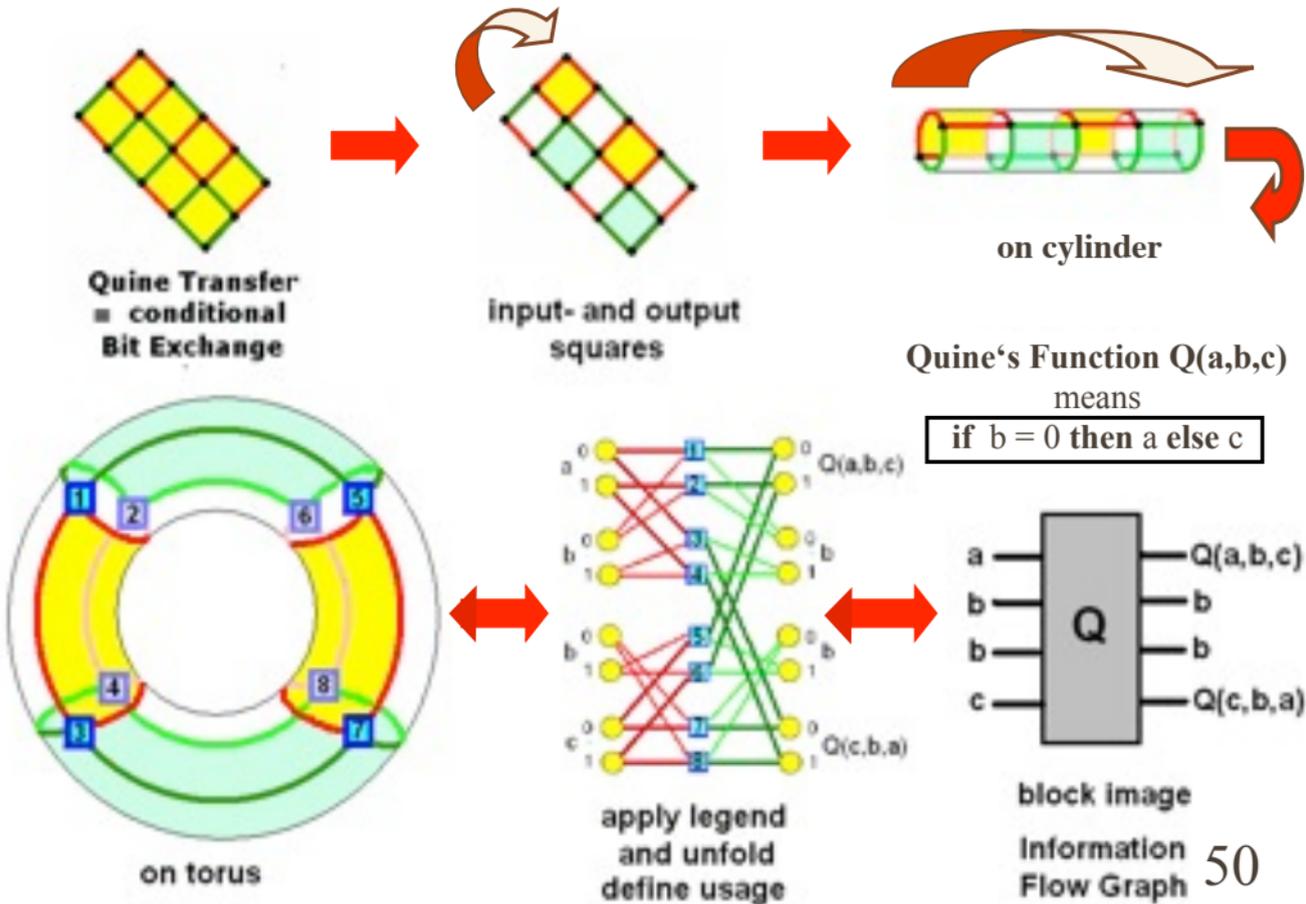


Quine Transfer = conditional Bit Exchange

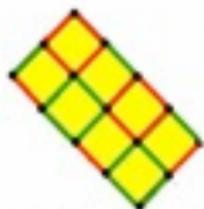
Legend:



How the Net constructs can be generated from the rough images



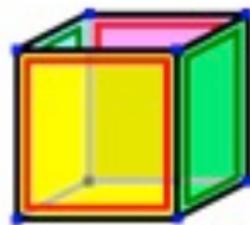
How the Net constructs can be generated from the rough images



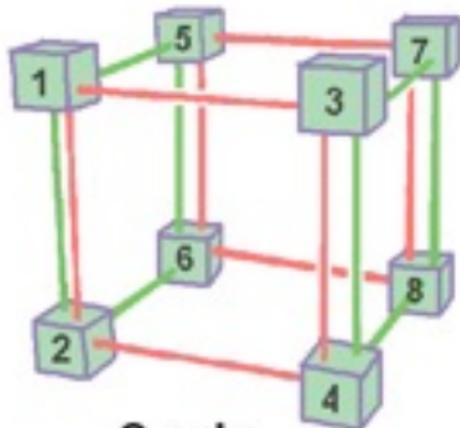
Quine Transfer
= conditional
Bit Exchange



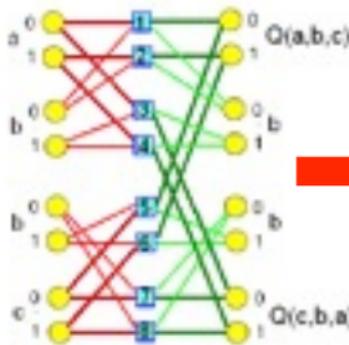
input- and output
squares



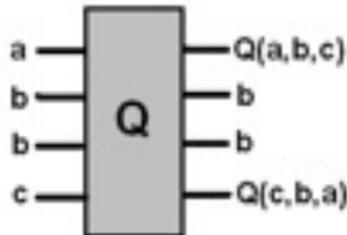
on a cube



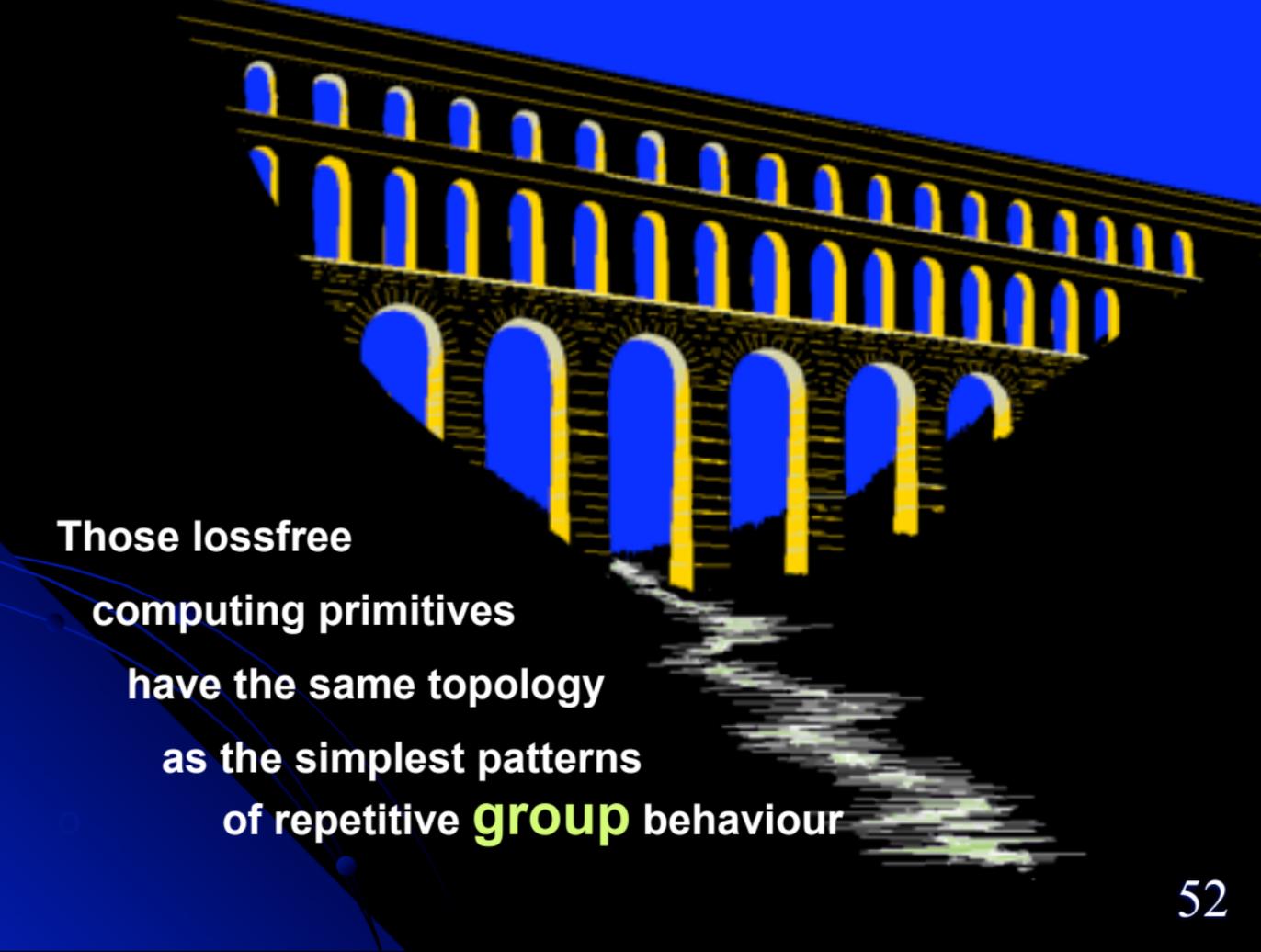
Q cube



apply legend
and unfold
define usage



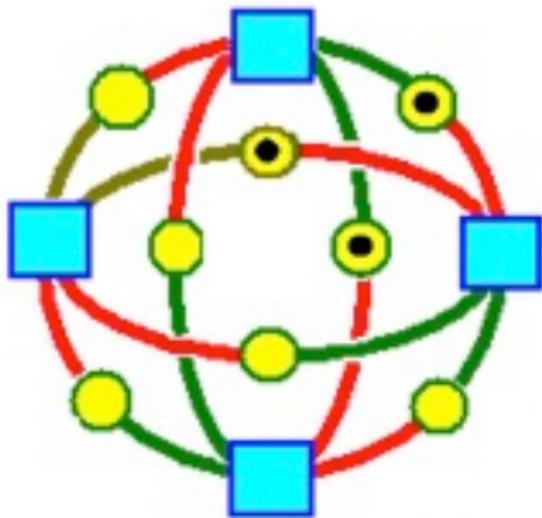
block image
Information
Flow Graph



Those lossfree
computing primitives
have the same topology
as the simplest patterns
of repetitive **group** behaviour

Different structures - same topology:

OSCILLATOR



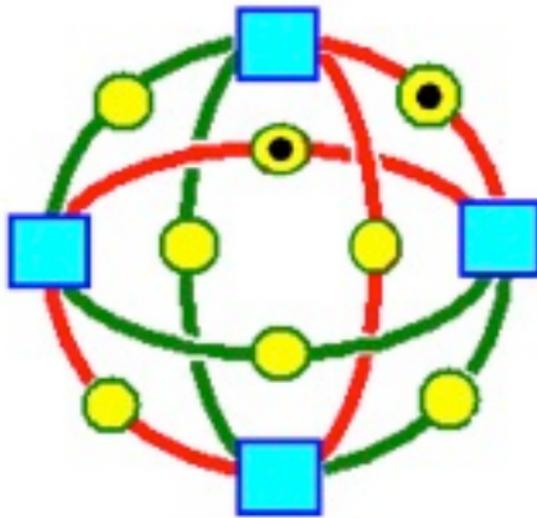
TAKE

GIVE

T-input

T-output

XOR



TAKE

GIVE

T-input

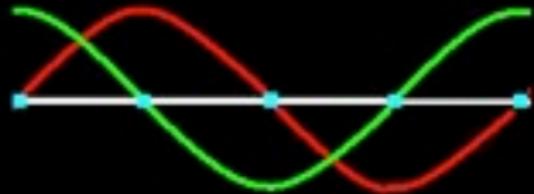
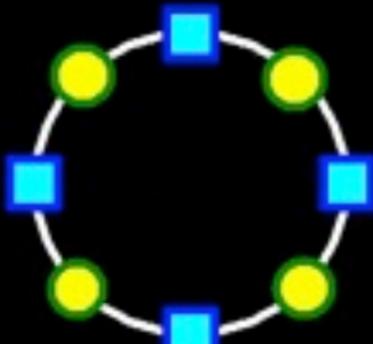
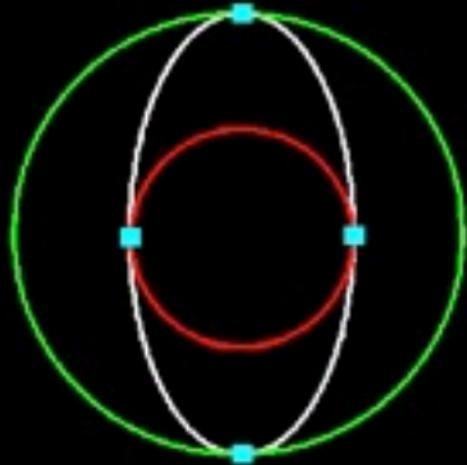
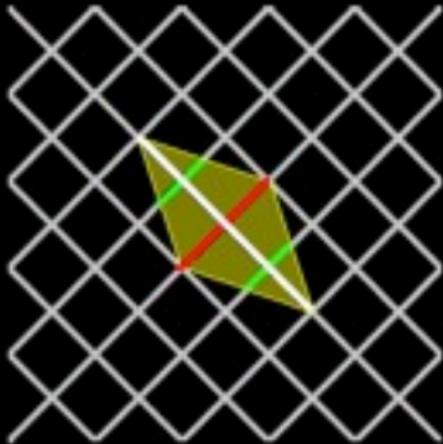
T-output

CONTINUOUS SPACES

continuous := connected and compact

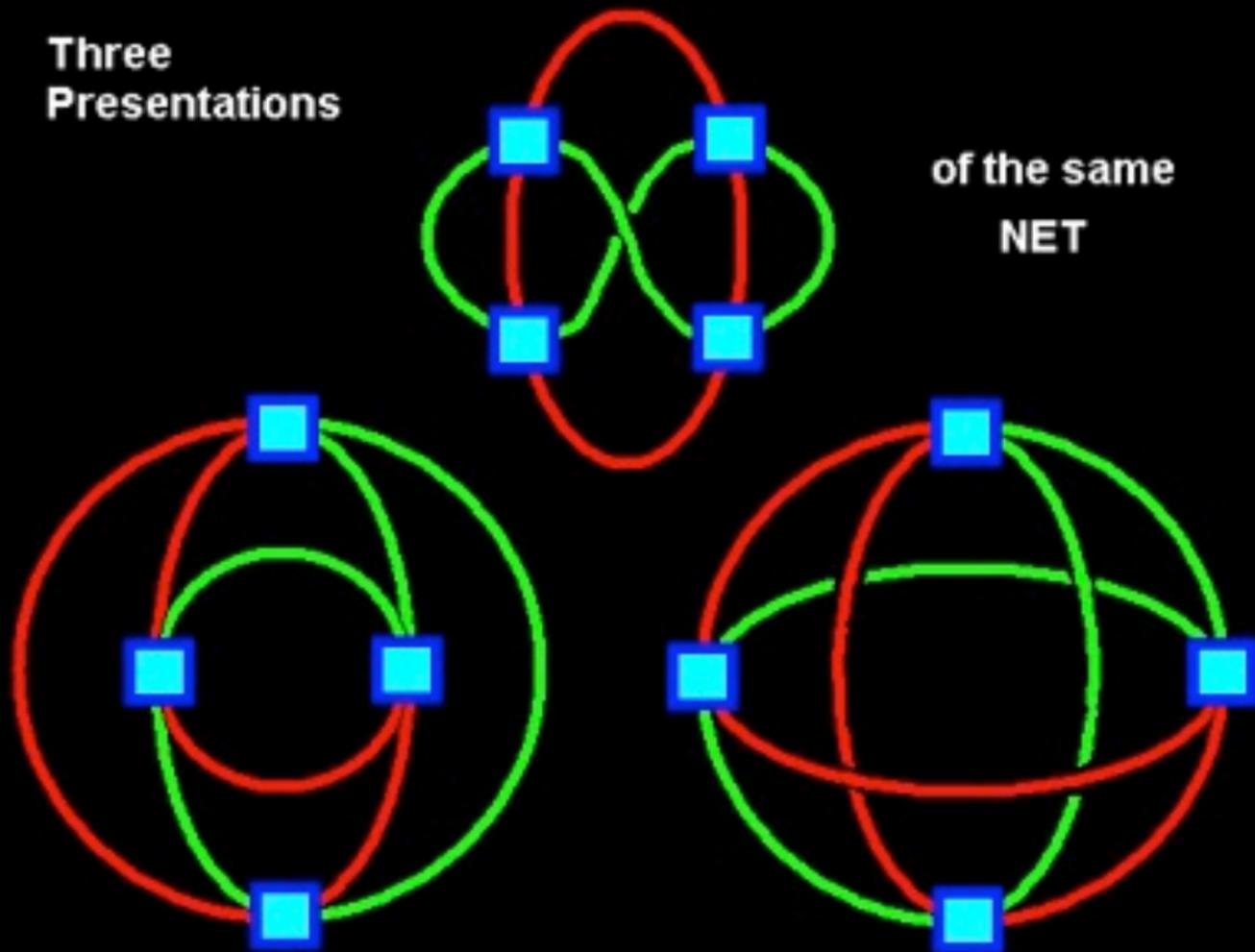
Structure	infinite	finite
$(\mathbb{R}, <)$ Real Numbers	Not Contin.	Not Contin.
$[0,1] \subset \mathbb{R}$ "Continuum"	Continuous	Not Contin.
$\mathbb{R} \cup \{\infty\}$ compactified	Continuous	Not Contin.
(S,T,F) Nets	Not Contin.	Continuous

Typical patterns we have considered:

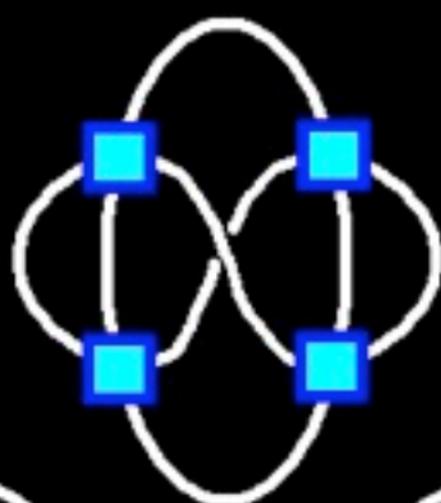


Three
Presentations

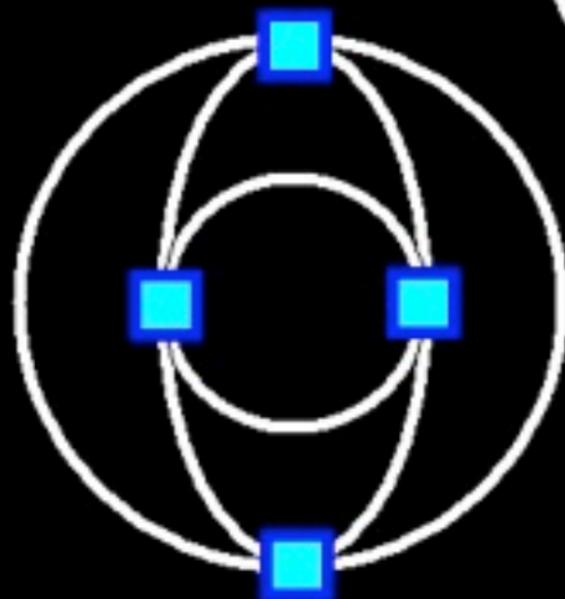
of the same
NET



Three
Presentations



of the same
Topology



Combinatorial Topologies

(such as connected Nets and Net Piles)

are Continuous Spaces
if and only if they are **Finite**.

that is, they share the properties
„connected“ and „compact“
with the Continuum of Real Numbers $[0,1]$

What follows from this main result ?

It follows that, if we base our models on the combinatorial concepts of signal flow suggested by Informatics, and **insist on continuity** (as Zuse did), we end up inevitably with a model of a Finite Universe.

Albert Einstein uttered the suspicion that the use of Real Numbers in general might **rest on an illusion**.

Many years later, Stephen Hawking adduced very strong reasons to confirm Einstein's doubt.

Today, there is a growing number of authors argueing in the direction of finite models of the univers!

What follows from this main result ?

In a finite world, can we use Analysis with a clean conscience?

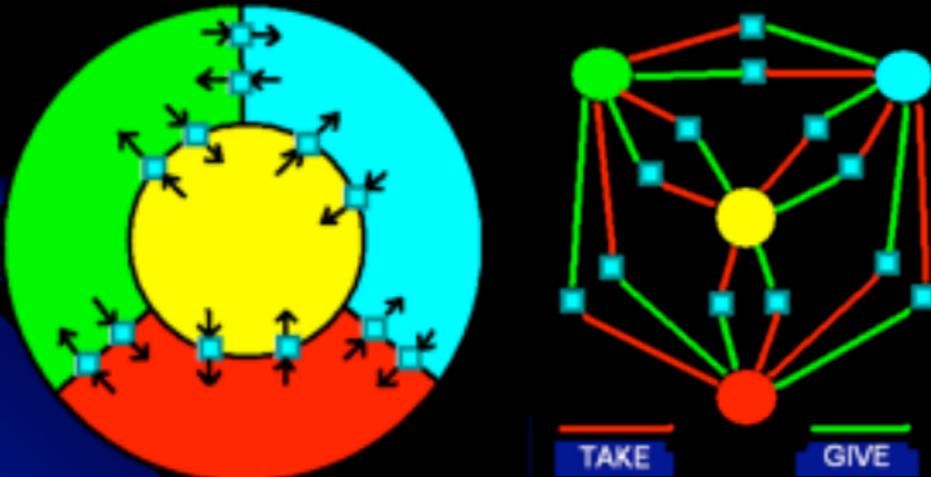
Definitely yes, if we do not forget that it is an **extrapolation of what can be experienced**.

We must not believe that we have
„Command and Control of the Infinite“.

We have to reject infinite results, and to consider the results of Analysis as good approximations of reality and **not** – contrary to widespread opinion – as more precise than observed reality.

Continuity in Finite Structures

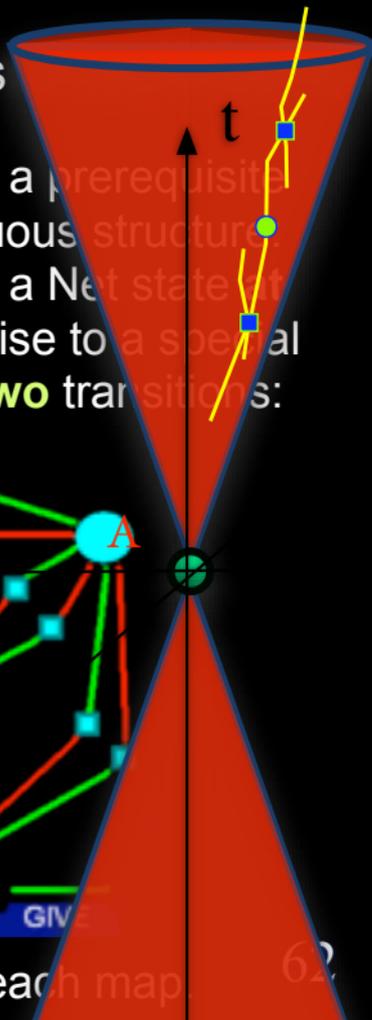
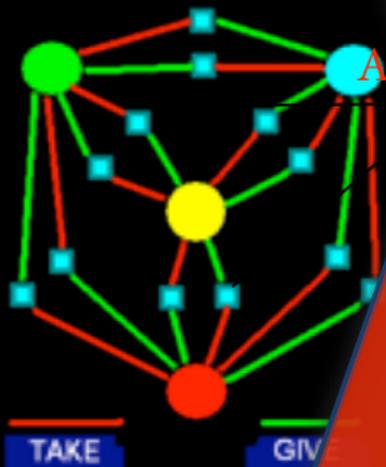
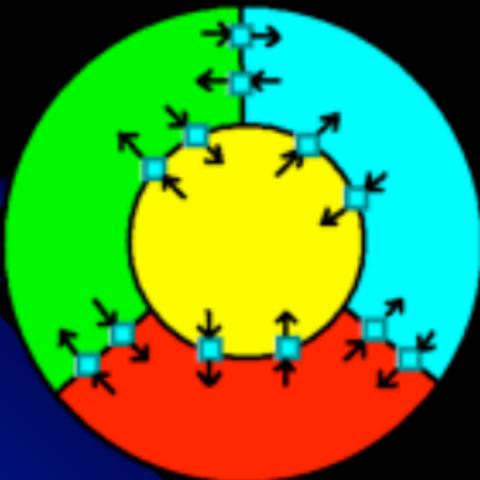
Contrary to widespread opinion, Infinity is not a prerequisite for Continuity. E.g. a political map is a continuous structure: Each state begins/ends at its borders, just as a Net state at the neighbouring transitions. The map gives rise to a special type of Net, and each piece of borderline to **two** transitions:



Any FINITE refinement can be applied to each map.

Continuity in Finite Structures

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Any FINITE refinement can be applied to each map.

For Zuse's „Computing Universe“,
this result suggests to assume a **Finite
Continuous Space without Boundary**

The Signal Flow Image is a 2-in 2-out
Net of size $2^{2^{2^{2^2}}} < 10^{20000}$

„without Boundary“
means
open *and* closed



for once, not digital.

For Zuse's „Computing Universe“,
this result suggests to assume a **Finite
Continuous Space without Boundary**.

The Information Flow Image is a smaller
Net: an S-arc graph of size $< 2^{2^{2^{2^2}}}$

„without Boundary“
means
open *and* closed



The Behaviour Net of this „Universe“ is **periodic** because of the finiteness of that Universe. Its size can be estimated as $2^{2^{2^{2^2}}}$.

It consists of cyclic **Signal Histories** over all time

If Information loss occurs, the Behaviour Net is not periodic, nor are the Signal Paths cyclic. **Determinism is still holding.**

ˆt Hooft likes that better ... And you ?
It is easy to **merge** some state pairs !





*Konrad Zuse disputing with Carl Adam Petri
about 1975*



Sceptical
audience
inspecting
Universe



Tobias
Petri

This lecture was based on the article

„Das Universum als großes Netz“

(in German) published in

SPEKTRUM DER WISSENSCHAFT

Special issue on the topic

„Ist das Universum ein Computer?“

SPEZIAL 3/07 (Nov. 2007)

Copies of full text of Petri's original lecture and
of a original much extending

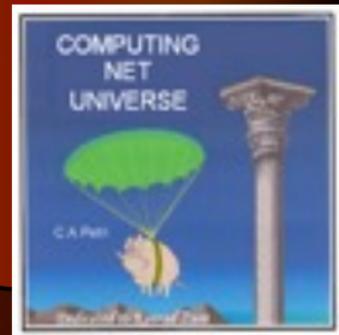
presentation (in English)

„COMPUTING NET UNIVERSE“ -

A continuation of the work of Konrad Zuse

available on CD

after this Lecture



THANK YOU!